tending the path for equivalent place wave propagation at low frequencies. This lengthenous can be evaluated quantitatively with the proposed method. This result is referent

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A Modal Parametric Method for Computing Acoustic Characteristics of Three-dimensional Vocal Tract Models

Kunitoshi MOTOKI*, Pierre BADIN**, Xavier PELORSON**
and Hiroki MATSUZAKI*

3.2. Configuration based on MRI daipartedA

A model for calculating the acoustic characteristics of three-dimensional vocal tract configuration is presented. A cascaded structure of rectangular acoustic tubes, connected asymmetrically with respect to their axes, is introduced as an approximation of the real vocal tract geometry. Both propagative and evanescent higher-order modes are considered in these tubes. The number of higher-order modes can be selected independently in each tube, which significantly decreases the instability of computation caused by the evanescent higher-order modes. Calculation results for two configurations are discussed.

1. Introduction

Recent development of techniques for the observation of speech organs such as MRI
allows us to obtain accurate descriptions of vocal tract shape. Although 3D shapes of the
vocal tract are available, 1D theories are still used to compute acoustic characteristics of
the vocal tract. A reason maybe lies in the complexity of computation of the resonance
characteristics of 3D shapes.

Numerical computation techniques such as the Finite Element Method (FEM) [1] or
the Transmission Line Matrix (TLM) method [2] have been applied to compute the
acoustic characteristics of 3D vocal tract models. The results obtained emphasize the
large influence of the vocal tract shape details upon the transfer function. These methods,

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however, require a large amount of computation, and are not suitable for the purpose of speech synthesis. I had a suitable for the purpose of speech synthesis.

This paper presents a parametric method to compute the acoustic characteristics of the 3D vocal tract model, in order to achieve the reduction of the computation, and to explore the vocal tract acoustics that can not be represented by the traditional 1D model. A cascaded structure of acoustic tubes, connected asymmetrically with respect to their axes, is introduced as an approximation of the vocal tract geometry. Each tube is assumed to have a rectangular cross-sectional shape whose geometry (size and axis position) can be determined from MRI data. The 3D acoustic field in each tube is represented in terms of higher-order modes. A mode-matching technique is then used to establish a mode coupling at the junctions between tubes. In the proposed method, both propagative and evanescent higher-order modes are considered in each tube, since each section is often not long enough for the evanescent modes to decay away.

Considering several evanescent higher-order modes sometimes causes computational difficulties related to the numerical precision. As a matter of fact, in a previous report [3], the number of higher-order modes taken into account in each tube was necessarily constant; this was a major drawback when constrictions were present since the evanescent higher-order modes in the narrow tube often caused computational instability. In the proposed method, the number of higher-order modes can be selected independently in each tube. In particular, only plane waves may be considered for narrow tubes and several higher-order modes can be taken into account for wider tubes. The flexibility in the selection of the number of the higher-order modes in each tube increases the computation stability significantly, while also reducing computational time.

Calculation results for two configurations, a 5-section configuration approximating an occlusion at the teeth, and 36-section configuration based on MRI data, are discussed.

2. 3D vocal tract model

2.1 Mode expansion and coupling

Vocal tracts are approximated by cascaded structures of rectangular acoustic tubes, as shown in figure 1. The 3D acoustic field in each tube can be represented in infinite series of higher-order modes. The sound-pressure p(x,y,z), z being the direction of the tube axis, and the z-direction particle velocity $v_z(x,y,z)$ in each tube are expressed as:

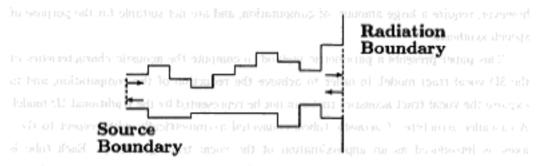


Figure 1. Example of vocal tract model.

For instance the
$$v_x(x,y,z) = \sum_{a,b=0}^{\infty} (a_{aa}e^{-\gamma a_{ab}x} + b_{aa}e^{\gamma a_{ab}x})\phi_{aa}(x,y)$$
 which is constant to be seen, we have the setting of $a_a = \int_{a_a}^{\infty} (a_a - a_a) da_b + D(z)dz$ where $a_a = \int_{a_a}^{\infty} (a_a - a_a) da_b + D(z)dz$ where $a_a = \int_{a_a}^{\infty} (a_a - a_a) da_b + D(z)dz$ and $a_a = \int_{a_a}^{\infty} (a_a - a_a) da_b$

where m and n stand for the numbers of the higher-order modes in x and y directions, γ_{mn} and $\phi_{mn}(x,y)$ are the propagation constant and normal function (eigen function), respectively. γ_{mn} 's are imaginary numbers for propagative modes and real numbers for evanescent modes. Neither loss factors due to the viscosity and the heat conductivity of air, nor wall vibration effects are included. In the matrix notation in eq. (1), the infinite series are truncated to a certain value. a, b and $\phi(x,y)$ are column vectors composed of a_{mn} , b_{mn} and $\phi_{mn}(x,y)$, respectively. $\phi_{mn}(x,y)$'s are chosen to have the following orthogonal property:

$$\frac{1}{S} \int_{S} \phi(x,y) \phi(x,y)^{T} dS = \mathbf{I}$$
 (2)

where S is the area of the tube, and I a unit matrix. **a** and **b** are determined by the boundary conditions at the both ends of each tube. D(z) and C_{C} are defined as:

$$\mathbf{D}(z) = \operatorname{diag}[\exp(\gamma_{nn}z)], \mathbf{Z}_c = jk\rho c(\operatorname{diag}[\gamma_{nn}])^{-1}$$
 (3)

where k, ρ and c are wave number, air density and sound speed, respectively. A modal sound-pressure vector \mathbf{P} and a modal particle velocity vector \mathbf{V} can be defined as:

$$\mathbf{P} = \mathbf{D}(-z)\mathbf{a} + \mathbf{D}(z)\mathbf{b}$$

$$\mathbf{V} = \mathbf{Z}z^{1}(\mathbf{D}(-z)\mathbf{a} - \mathbf{D}(z)\mathbf{b})$$
(4)

If each component of P and V is regarded as a voltage and a current at position z, each higher-order mode can be represented by an equivalent electrical transmission line.

Hereafter, a subscript i is used to represent the variables in the section i. By using a mode matching technique, the mode coupling at the junction between the sections i and i+1 can be expressed as follows[4]:

$$\mathbf{P}_{t} = \mathbf{\Phi}_{t,t+1} \mathbf{P}_{t+1}$$

$$\mathbf{\Phi}_{t,t+1}^{T} \mathbf{V}_{t} = \mathbf{V}_{t+1}$$
(5)

where the coupling matrix $\Phi_{i,i+1}$ is calculated as:

$$\Phi_{i,i+1} = \frac{1}{S_i} \int_{S_i} \phi_i(x,y) \phi I_{+1}(x,y) dS$$
 (6)

 S_i is assumed to be smaller than that of the section i+1. If the smaller area is for section i+1, all suffixes i and i+1 should just be exchanged. Equation (5) indicates that the coupling coefficients matrix $\Phi_{i,i+1}$ can be simply regarded as a matrix representing the transformation ratio of a multi-port ideal transformer in an equivalent electrical circuit.

2.2 Impedance transformation

Acoustic transfer functions and sound-pressure distributions in the vocal tract can be calculated from input impedance matrices at each section. Starting with a given load impedance matrix, which is often a radiation impedance matrix, an impedance transformation is necessary to obtain the input impedance matrices for all sections. Kergomard [4] presented a "propagating modes" method for the impedance transformation where all evanescent modes are terminated at the junction. In this section, the formulation of the impedance transformation suitable for the 3D vocal-tract model is presented. It can handle short sections with asymmetrical connection between the adjacent tubes. It should be noted that the evanescent higher-order modes do not propagate. However, they can influence the resonance characteristics through the mode coupling between plane waves and the evanescent modes at the junction. Moreover, if two junctions are located very closely, the evanescent modes can be related to a power transmission. Thus we consider the evanescent modes either as "terminated" at the junction or as "related to the power transmission" in the tube as illustrated in figure 2.

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"X "A radiation impedance matrix is the first impedance for starting the impedance transformation. The generalized modal radiation impedance matrix \mathbf{Z}_{rad} for a rectangu-

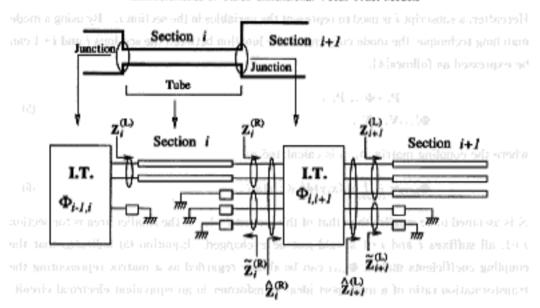


Figure 2. Equivalent electrical circuit.

lar opening with the higher-order modes is given by [5] as: should release to the higher-order modes is given by [5].

require the strikest variable questions are the strikest of variable and strikest
$$Z_{mn,pq} = \frac{jk\rho c}{2\pi S} \int_{A} \int_{A} \phi_{mn}(x_{i}y)\phi_{pq}(x'_{i}y') \frac{e^{-ik\tau}}{r} dS'dS_{r}$$
 in the set v have a result of (7).

$$Z_{mn,bq} = \frac{R_{pq}}{2\pi S} \int_{S} \int_{S} \phi_{mn}(x,y) \phi_{pq}(x',y') \frac{dy}{y} dS'dS$$
, in the of where where (7) relations of examples $x_{pq} = \frac{1}{2\pi S} \int_{S} \int_{S} \phi_{mn}(x,y) \phi_{pq}(x',y') \frac{dy}{y} dS'dS$, in the of where where (7)

where S is the area of the last section corresponding to the mouth. Note that Z_{mappy} represents the modal radiation impedance between modes (m,n) and (p,q). Z_{0000} is the radiation impedance used in the plane wave theory, undeled appropriate and unit before ad-

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Tube Input impedances looking toward loads at the right and left ends of the section i are defined as: a leasable as no unarount esta by "teananarea" as matter solvent trackens or with

$$\mathbf{P}_{t}^{(0)} = \mathbf{Z}_{t}^{(0)} \mathbf{V}_{t}^{(0)}, \quad \mathbf{P}_{t}^{(1)} = \mathbf{Z}_{t}^{(1)} \mathbf{V}_{t}^{(1)}$$
 (8)

where superscripts (8) and (4.) are used to denote the quantities at the right (lip side) and left (glottis side) ends of the tube. From eq. (4), the impedance transformation from Z⁽ⁿ⁾ to Z⁽ⁿ⁾ transformation. The generalized model radiation improbase matrices bankton vises at

$$\mathbf{Z}_{i}^{(L)} = (\mathbf{D}_{C_{i}}\mathbf{Z}_{i}^{(0)} + \mathbf{D}_{S_{i}}\mathbf{Z}_{C_{i}})(\mathbf{D}_{S_{i}}\mathbf{Z}_{i}^{(0)} + \mathbf{D}_{C_{i}}\mathbf{Z}_{C_{i}})^{-1}\mathbf{Z}_{C_{i}}$$
(9)

where $\mathbf{D}_{t_i} = {\mathbf{D}_i(L_i) + \mathbf{D}_i(-L_i)}/2$ and $\mathbf{D}_{t_i} = {\mathbf{D}_i(L_i) - \mathbf{D}_i(-L_i)}/2$, L_i being the length of the section i.

Junction of the relation between impedance matrices of Z⁽⁰⁾ and Z⁽⁰⁾ is given from the well-known circuit theory as: 100-110 but the Director between the business of the

The entropy is although the matter
$$\mathbf{Z}_{i}^{(0)} = \mathbf{\Phi}_{i,i+1} \mathbf{Z}_{i+1}^{(1)} \mathbf{\Phi}_{i,i+1}^{(1)}$$
 and the matter $\mathbf{Z}_{i}^{(0)} = \mathbf{\Phi}_{i,i+1} \mathbf{Z}_{i+1}^{(1)} \mathbf{\Phi}_{i,i+1}^{(1)}$ and the results of the superal value of the superal v

or 2.2.3 Transformation with terminations of bulled at their growing out of all a second

We assume that the coupling coefficient matrix $\Phi_{i,i+1}$ is square. The number of modes selected for the calculation of $\Phi_{i,i+1}$ can be large. It may be, however, limited to 5 or 6 as described in the next section. Some of these modes are considered for transmission, while the others are terminated with their characteristic impedances as illustrated in figure 2. Some input impedance matrices are also defined in figure 2. The problem to solve for the impedance transformation is to express $\mathbf{Z}_{i}^{(t)}$ in terms of $\hat{\mathbf{Z}}_{i}^{(t)}$, $\mathbf{Z}_{i+1}^{(t)}$ and $\hat{\mathbf{Z}}_{i+1}^{(t)}$, $\hat{\mathbf{Z}}_{i+1}^{(t)}$ are simply diagonal matrices composed of characteristic impedances used for termination of the ideal transformer. $\hat{\mathbf{Z}}_{i+1}^{(t)}$ is written as,

$$\hat{\mathbf{Z}}_{(2)}^{(2)} = \begin{bmatrix} \mathbf{Z}_{(2)}^{(2)} & \mathbf{0} \\ \mathbf{0} & \tilde{\mathbf{Z}}_{(2)} \end{bmatrix} \tag{11}$$

Then from eq. (10), we get,

$$\bar{Z}_{i}^{(t)} = \Phi_{i,i+1} \bar{Z}_{i-1}^{(t)} \Phi_{i,i+1}^{T}$$
 (12)

 $\hat{\mathbf{Z}}_{i}^{(n)}$ can be decomposed into sub matrices as:

$$\bar{\mathbf{Z}}_{1}^{(k)} = \begin{bmatrix} \bar{\mathbf{Z}}_{1,1}^{(k)} & \bar{\mathbf{Z}}_{1,2}^{(k)} \\ \bar{\mathbf{Z}}_{1,2}^{(k)} & \bar{\mathbf{Z}}_{1,2}^{(k)} \end{bmatrix}$$
(13)

where the size of $\mathbf{Z}_{i,n}^{(n)}$ corresponds to the number of modes considered for transmission in the *i*-th section. Then $\mathbf{Z}_{i,n}^{(n)}$ is calculated as: $\mathbf{z}_{i,n}^{(n)} = \mathbf{z}_{i,n}^{(n)}$ is calculated as:

$$\mathbf{Z}_{1}^{(0)} = \tilde{\mathbf{Z}}_{1,1}^{(0)} - \tilde{\mathbf{Z}}_{1,12}^{(0)} (\tilde{\mathbf{Z}}_{1,22}^{(0)} + \tilde{\mathbf{Z}}_{1}^{(0)})^{-1} \tilde{\mathbf{Z}}_{1,21}^{(0)}$$
(14)

Finally, $\mathbf{Z}_{i}^{(t)}$ is obtained by substituting $\mathbf{Z}_{i}^{(t)}$ into eq. (9). Repeating the above procedure section by section, the given radiation impedance matrix \mathbf{Z}_{red} in eq. (7) is transformed into the input impedance matrix of the first section.

2.3 Transfer function

Once all input impedance matrices are obtained, wave component vectors \mathbf{a} and \mathbf{b} at each section can be calculated using eqs. (4) and (5) recursively. Then sound-pressure distribution is obtained from eq. (1). It is also possible to compute the sound-pressure at an arbitrary far point by using the Rayleigh integral with the calculated vibrating pattern at the radiation end. However, a more convenient way to evaluate the resonance characteristics is to use the power that is actually radiated in the free space. Since the present model assumes no losses inside the vocal tract, the actual radiation power is equal to the total active intensities W_i on any arbitrary cross-section in tubes, which can be evaluated at the glottis section as:

$$W_{i} = \int_{t_{i}} \frac{1}{2} \operatorname{Re}(p_{i}^{*} v_{z_{i}}) dS = \frac{S_{i}}{2} \operatorname{Re}\{(\mathbf{Z}^{(1)} \mathbf{V}^{(1)})^{*} \mathbf{V}^{(1)}\}$$
(15)

where * denotes a complex conjugate, and V_i is the modal particle velocity vector of the given pattern of the source vibration. Then the sound-pressure at a far point can be considered to be proportional to $\sqrt{W_i}$. Thus the transfer function H of the proposed model is evaluated by,

$$H \propto \frac{\sqrt{W_t}}{U_0}$$
 (16)

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where U_6 is a source volume velocity.

3. Results

3.1 Configuration with 5-section

A 5-section configuration is used to imitate the occlusion at the teeth as illustrated in figure 3. A tiny square sound source (0.01 mm × 0.01mm) is located at 0.5 mm apart from the upper right corner. In the narrow sections 2 and 4 only plane waves are considered for the transmission and the first 2 higher-order modes (1,0) and (2,0) are considered for the mode coupling at each junction. Computed sound-pressure distribution at 1 kHz is shown in figure 4, both amplitude and phase contours being presented. Note that these higher-

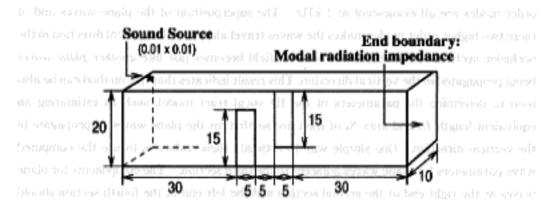


Figure 3. 5-section configuration.

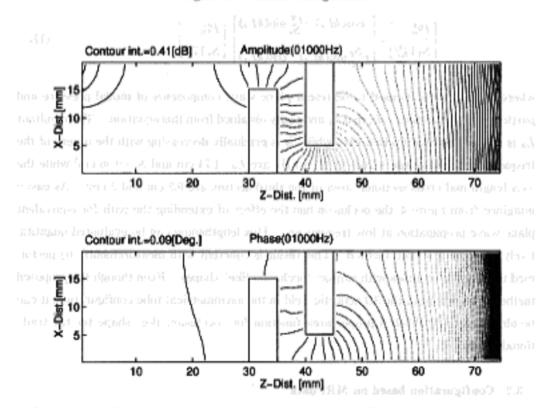


Figure 4. Sound-pressure distributions at 1kHz.

Figure 4. Sound-pressure distribution at 1kHz.

Figure 4. Sound-pressu

order modes are all evanescent at 1 kHz. The superposition of the plane waves and of these two higher-order modes makes the waves travel almost in the vertical direction in the occlusion section. As a result, the acoustic field becomes just like another plane waves being propagated in the vertical direction. This result indicates that this method can be also used to determine the parameters of the 1D vocal tract model, such as estimating an equivalent length L_{ℓ} and area S_{ℓ} of the third section for the plane waves to propagate in the vertical direction. One simple way to estimate these values is to use the computed wave parameters for plane waves adjacent to the third section. The components for plane waves at the right end of the second section and the left end of the fourth section should be related by L_{ℓ} and S_{ℓ} with the plane wave theory as:

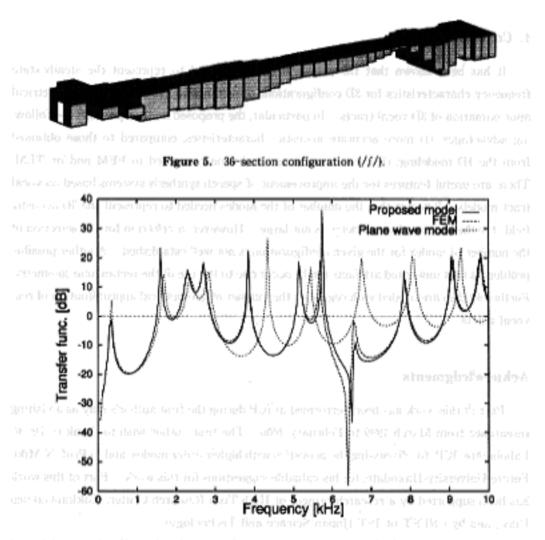
$$\begin{bmatrix}
P_{2st}^{(R)} \\
S_2 V_{2ss}^{(R)}
\end{bmatrix} = \begin{bmatrix}
\cos(kL_e) & j \frac{PC}{S_e} \sin(kL_e) \\
j \frac{S_e}{aC} \sin(kL_e) & \cos(kL_e)
\end{bmatrix} \begin{bmatrix}
P_{4so}^{(L)} \\
S_4 V_{4ss}^{(L)}
\end{bmatrix}$$
(17)

where the suffix " $_{\infty}$ " is used to represent plane wave components of modal pressure and particle velocity vectors. L_e and S_e are easily obtained from this equation. The resultant L_e is almost constant up to 6 kHz while S_e is gradually decreasing with the ascent of the frequency. The average values up to 5 kHz are $L_e=1.74$ cm and $S_e=0.56$ cm² while the axis length and cross-sectional area of the third section are 0.5 cm and 2 cm². As easily imagined from figure 4, the occlusion has the effect of extending the path for equivalent plane wave propagation at low frequencies. This lengthening can be evaluated quantitatively with the proposed method. This result is coherent with measurements [6] performed using circular tubes with similar "occlusion-like" shapes. Even though the proposed method is to represent the 3D acoustic field in the asymmetrical tube configuration, it can be also used to establish a proper area function for "occlusion-like" shape for the traditional 1D model.

3.2 Configuration based on MRI data

In order to study the differences between the plane wave and the higher-order models, the 3D shape of a /// measured by MRI has been converted into a 36-section configuration as illustrated in figure 5. Each tube is aligned to a common horizontal plane. The entire configuration is symmetrical with respect to the lateral direction, but asymmetrical in the vertical direction. A sound source is assumed to be located at the beginning of the first

section. 5 higher-order modes (3 in lateral direction and 2 in vertical direction) are considered at each junction. Figure 6 shows the acoustic transfer characteristics defined in eq. (16) together with those obtained from the FEM simulation and from the 1D model. The peak frequencies obtained by the proposed method agree well with those from the FEM although a slight difference around a "zero" at 6.4 kHz is seen. The frequency of the zero tends to be more sensitive to the number of the higher-order modes than the peak frequencies. For peak frequencies up to 5 kHz, only a few higher-order modes are necessary to give the same peak frequencies as those of FEM. Comparison with the result of



hum address and a Figure 6.44 Transfer functions of 36-section configuration. A security with

the 1D model suggests that the resonance frequencies are always lowered due to the evanescent higher-order modes. The rates of shift relative to the 1D model for the first 4 resonance frequencies are +3.8, +4.0, +3.1, and +4.3%, respectively. Above the 5-th resonance frequency, the plane wave and the higher-order models have quite different transfer characteristics. The "zero" can appear around the first cut-off frequency in the lateral direction of the widest section. This may be understood using the analogy with side branches, since the higher-order modes in each section correspond to transmission lines in parallel as an equivalent electrical circuit.

4. Conclusion

It has been shown that the proposed model is valid to represent the steady-state frequency characteristics for 3D configurations of rectangular tubes used as a geometrical approximation of 3D vocal tracts. In particular, the proposed method presents the following advantages: (1) more accurate acoustic characteristics, compared to those obtained from the 1D modeling; (2) shorter computational time compared to FEM and/or TLM. These are useful features for the improvement of speech synthesis systems based on vocal tract models. It seems that the number of the modes needed to represent the 3D acoustic field for the rectangular geometry is not large. However, a criterion for the selection of the number of modes for the given configuration is not well established. Another possible problem is that unwanted artifacts might occur due to the use of the rectangular geometry. Further studies are needed with regard to the manner of geometrical approximation of real vocal tracts.

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